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# **hypercube Documentation**

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# CHAPTER 1

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## Introduction

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hypercube is a package for reasoning about Radio Interferometry problem sizes.

Radio Interferometry data, such as visibilities, is both large and dense. Computation on this data is therefore generally suited to distributed, data parallel computation. To achieve this parallelism it is necessary to subdivide this data into tiles, large enough to fit within the memory budgets of individual nodes and GPUs.

hypercube is an simple abstraction that uses labelled Dimensions and abstract `numpy` array shapes, defined in terms of these Dimensions, to:

- Reason about memory budgets
- Choose array subdivision strategies
- Iterate over a problem space

```
from hypercube import HyperCube

cube = HyperCube()
cube.register_dimension("ntime", 10000,
    description="Timesteps")
cube.register_dimension("nbl", 2016,
    description="Baselines")
cube.register_dimension("nchan", 16384,
    description="Channels")

cube.register_array("uvw", ("ntime", "nbl", 3),
    np.float64)
cube.register_array("frequency", ("nchan",),
    np.float64)
cube.register_array("model_vis", ("ntime", "nbl", "nchan", 4),
    np.complex128)
```

```
print cube
```

```
Registered Dimensions:
Dimension Name      Description      Global Size  Extents
```

nbl	Baselines	2016	(0, 2016)
nchan	Channels	16384	(0, 16384)
ntime	Timesteps	10000	(0, 10000)
Registered Arrays:			
Array Name	Size	Type	Shape
frequency	128.0KB	float64	(nchan)
model_vis	19.2TB	complex128	(ntime,nbl,nchan,4)
uvw	461.4MB	float64	(ntime,nbl,3)
Local Memory Usage	19.2TB		



## Dimensions

The use of `python` and `numpy` in the Radio Astronomy community naturally results in representation of data as multi-dimensional `numpy` arrays. `hypercube`, similarly to `xray` and `pandas` utilises the concept of labelling Dimensions. For example, a `hypercube` can be created and **Time**, **Baseline**, and **Channel** dimensions can be registered with various global sizes.

```
from hypercube import HyperCube

cube = HyperCube()
cube.register_dimension("ntime", 10000,
    description="Timesteps")
cube.register_dimension("nbl", 2016,
    description="Baselines")
cube.register_dimension("nchan", 16384,
    description="Channels")
```

Printing the cube then yields information about the registered Dimensions. Note that the **Global Size** matches the **Extents**.

```
print cube
```

Registered Dimensions:

Dimension Name	Description	Global Size	Extents
nbl	Baselines	2016	(0, 2016)
nchan	Channels	16384	(0, 16384)
ntime	Timesteps	10000	(0, 10000)

## Arrays

Then we can register an abstract definition, or schema, of the **Model Visibility** array on the hypercube defined using the names of the previously registered dimensions.

```
cube.register_array("uvw", ("ntime", "nbl", 3), np.float64)
cube.register_array("frequency", ("nchan",), np.float64)
cube.register_array("model_vis", ("ntime", "nbl", "nchan", 4),
    np.complex128)
```

Printing the cube now displays additional information about the arrays and their sizes in terms of the dimension **extents**.

Registered Dimensions:			
Dimension Name	Description	Global Size	Extents
-----	-----	-----	-----
nbl	Baselines	2016	(0, 2016)
nchan	Channels	16384	(0, 16384)
ntime	Timesteps	10000	(0, 10000)
Registered Arrays:			
Array Name	Size	Type	Shape
-----	-----	-----	-----
frequency	128.0KB	float64	(nchan)
model_vis	19.2TB	complex128	(ntime,nbl,nchan,4)
uvw	461.4MB	float64	(ntime,nbl,3)
Local Memory Usage	19.2TB		

## Modifying Dimension Extents

The problem in the previous section is too large (19.2TB) to fit within a single compute node's memory, so it is necessary to subdivide or tile the problem. The **extents** of the **Time** and **Channel** dimension are modified as follows:

```
cube.update_dimension("ntime", lower_extent=0, upper_extent=100)
cube.update_dimension("nchan", lower_extent=0, upper_extent=64)

print cube
```

Registered Dimensions:			
Dimension Name	Description	Global Size	Extents
-----	-----	-----	-----
nbl	Baselines	2016	(0, 2016)
nchan	Channels	16384	(0, 64)
ntime	Timesteps	10000	(0, 100)
Registered Arrays:			
Array Name	Size	Type	Shape
-----	-----	-----	-----
frequency	512.0B	float64	(nchan)
model_vis	787.5MB	complex128	(ntime,nbl,nchan,4)
uvw	4.6MB	float64	(ntime,nbl,3)
Local Memory Usage	792.1MB		

Note how the dimension extents of the **Time** and **Channel** dimensions have changed. The problem now fits within a reasonable memory budget of 792.1MB.

## Querying Dimension Extents

The dimension extents can be queried on the cube:

```
cube.dim_lower_extent("ntime,nbl,nchan")
[0, 0, 0]

cube.dim_upper_extent("ntime,nbl,nchan")
[100, 2016, 64]

cube.dim_extent_size("ntime,nbl,nchan")
[100, 2016, 64]

cube.dim_extents("ntime,nbl,nchan")
[(0, 100), (0, 2016), (0, 64)]
```

## Iterating over Cubes

The cube supports iteration over tiles defined by dimensions. The `hypercube.base_cube.HyperCube.extent_iter()` method produces tuples of lower extents for each dimension provided to it. Here, it produces extents for tiles of 100 Timesteps and 64 Channels.

```
for (lt, ut), (lc, uc) in cube.extent_iter(("ntime", 100), ("nchan", 64)):
    print ("lower time {} upper time {} "
          "lower channel {} upper channel {}".format(
              lt, ut, lc, uc))

lower time 0 upper time 100 lower channel 0 upper channel 64
lower time 0 upper time 100 lower channel 64 upper channel 128
lower time 0 upper time 100 lower channel 128 upper channel 192
lower time 0 upper time 100 lower channel 192 upper channel 256
lower time 0 upper time 100 lower channel 256 upper channel 320
```

Other methods of iteration include producing dictionaries defining dimension updates

```
for d in cube.dim_iter(("ntime", 100), ("nchan", 64)):
    print d
    cube.update_dimensions(d)

({'lower_extent': 0, 'upper_extent': 100, 'name': 'ntime'},
 {'lower_extent': 64, 'upper_extent': 128, 'name': 'nchan'})
```

and producing cubes defining the tile on each iteration

```
for c in cube.dim_iter(("ntime", 100), ("nchan", 64)):
    ...
```



## Dimension

**class** **Dimension** (*name, global\_size, lower\_extent=None, upper\_extent=None, description=None*)

The Dimension class describes a hypercube dimension.

**\_\_init\_\_** (*name, global\_size, lower\_extent=None, upper\_extent=None, description=None*)

Create a Dimension from supplied arguments

### Parameters

- **name** (*str*) – Dimension name
- **global\_size** (*int*) – Global dimension size
- **local\_extent** (*int*) – Lower dimension extent
- **upper\_extent** (*int*) – Upper dimension extent
- **description** (*str*) – Dimension description

**copy** ()

### Returns

**Return type** A copy of the dimension

**description**

Dimension description

**extent\_size**

Size of the dimension extents. Equal to *upper\_extent - lower\_extent*

**global\_size**

Global dimension size

**lower\_extent**

Lower dimension extent

**name**

Dimension name

**update** (*global\_size=None, lower\_extent=None, upper\_extent=None, description=None*)

Update the dimension properties

#### Parameters

- **global\_size** (*int*) – Global dimension size (Default value = None)
- **lower\_extent** (*int*) – Lower dimension extent (Default value = None)
- **upper\_extent** (*int*) – Upper dimension extent (Default value = None)
- **description** (*str*) – Dimension description (Default value = None)

**upper\_extent**

Upper dimension extent

**validate** ()

Validate the contents of a dimension data dictionary

## HyperCube

**class HyperCube** (*\*args, \*\*kwargs*)

Hypercube.

**\_\_init\_\_** (*\*args, \*\*kwargs*)

Hypercube Constructor

**array** (*name, reify=False*)

```
cube.register("uvw", ("ntime", "na", 3), np.float64)

cube.array("uvw", reify=False)["shape"] == ("ntime", "na", 3)
cube.array("uvw", reify=True)["shape"] == (100, 7, 3)
```

#### Parameters

- **name** (*str*) – Array name
- **reify** (*bool*) – If True, converts abstract array schemas into concrete shapes.

**Returns** An array dictionary

**Return type** `dict`

**array\_extents** (*array\_name, \*\*kwargs*)

Return a list of lower and upper extents for the given array\_name.

```
cube.register("uvw", ("ntime", "na", 3), np.float64)

(lt, ut), (la, ua), (_, _) = cube.array_extents("uvw")
```

**Parameters** **array\_name** (*string*) – Name of an array registered on this hypercube

**Returns** List of (lower\_extent, upper\_extent) tuples associated with each array dimension

**Return type** `list`

**array\_slice\_index** (*array\_name*, *\*\*kwargs*)

Returns a tuple of slices, each slice equal to the slice(lower\_extent, upper\_extent, 1) of the dimensions of array\_name.

```
cube.register("uvw", ("ntime", "na", 3), np.float64)

idx = cube.array_slice_index("uvw")
uvw[idx].sum()
ntime, na, components = cube.array_slice_index("uvw")
A[ntime, na, components].sum()
```

**Parameters** **array\_name** (*str*) – Name of the array on this cube to slice

**Returns** Tuple of slice(lower, upper, 1) objects

**Return type** tuple

**arrays** (*reify=False*)

**Parameters** **reify** (*bool*) – If True, converts abstract array schemas into concrete shapes.

**Returns** A dictionary of array dictionaries, keyed on array name

**Return type** dict

**bytes\_required** ()

**Returns** Estimated number of bytes required by arrays registered on the cube, taking their extents into account.

**Return type** int

**copy** ()

**Return type** Return a copy of the hypercube

**cube\_iter** (*\*dim\_strides*, *\*\*kwargs*)

Recursively iterate over the (dimension, stride) tuples specified in dim\_strides, returning cloned hypercubes with each of the specified dimensions modified accordingly.

For example, the following call effectively produces 2 loops over the ‘ntime’ and ‘nchan’ dimensions in chunks of 10 and 4 respectively.:

```
A = np.ones(size=(100, 4))
for c in cube_iter(('ntime', 10), ('nchan', 4))
    assert c.dim_extent_size('ntime', 'nchan') == (10, 4)
```

**Parameters** **\*dim\_strides** (*list*) – list of (dimension, stride) tuples

**Returns** Iterator producing hypercubes

**Return type** iterator

**dim\_extent\_size** (*\*args*, *\*\*kwargs*)

Returns extent sizes of the dimensions in args.

```
ts, bs, cs = cube.dim_extent_size('ntime', 'nbl', 'nchan')
```

or

```
ts, bs, cs, ss = cube.dim_extent_size('ntime,nbl:nchan nsrc')
```

**dim\_extents** (\*args, \*\*kwargs)

Returns extent tuples of the dimensions in args.

```
(tl, tu), (bl, bu) = cube.dim_extents('ntime', 'nbl')
```

or

```
(tl, tu), (bl, bu) = cube.dim_upper_extent('ntime,nbl')
```

**dim\_global\_size** (\*args, \*\*kwargs)

Return the global size of the dimensions in args.

```
ntime, nbl, nchan = cube.dim_global_size('ntime', 'nbl', 'nchan')
```

or

```
ntime, nbl, nchan, nsrc = cube.dim_global_size('ntime,nbl:nchan nsrc')
```

**dim\_global\_size\_dict** ()

Returns a mapping of dimension name to global size

**dim\_iter** (\*dim\_strides, \*\*kwargs)

Recursively iterate over the (dimension, stride) tuples specified in dim\_strides, returning a tuple of dictionaries describing a dimension update.

For example, the following call effectively produces 2 loops over the 'ntime' and 'nchan' dimensions in chunks of 10 and 4 respectively.

```
for d in cube.dim_iter(('ntime', 10), ('nchan', 4)):
    cube.update_dimensions(d)
```

**Parameters** \*dim\_stride (*list*) – list of (dimension, stride) tuples

**Returns** Iterator produces dictionaries describing dimensions updates. {'name': 'ntime', 'lower\_extent': 100, 'upper\_extent': 200 }

**Return type** iterator

**dim\_lower\_extent** (\*args, \*\*kwargs)

Returns the lower extent of the dimensions in args.

```
t_ex, bl_ex, ch_ex = cube.dim_lower_extent('ntime', 'nbl', 'nchan')
```

or

```
t_ex, bl_ex, ch_ex, src_ex = cube.dim_lower_extent('ntime,nbl:nchan nsrc')
```

**dim\_lower\_extent\_dict** ()

Returns a mapping of dimension name to lower\_extent

**dim\_upper\_extent** (\*args, \*\*kwargs)

Returns the upper extent of the dimensions in args.

```
t_ex, bl_ex, ch_ex = cube.dim_upper_extent('ntime', 'nbl', 'nchan')
```



or

```
t_ex, bl_ex, ch_ex, src_ex = cube.dim_upper_extent('ntime,nbl:nchan nsrc')
```

**dim\_upper\_extent\_dict()**

Returns a mapping of dimension name to upper\_extent

**dimension** (*name*, *copy=True*)

Returns the requested *Dimension* object

**Parameters**

- **name** (*str*) – Name of the *Dimension* object
- **copy** (*boolean*) – Returns a copy of the *Dimension* object if True (Default value = True)

**Returns** A *Dimension* object.

**Return type** *Dimension*

**dimensions** (*copy=True*)

Return a dictionary of *Dimension* objects.

**Parameters** **copy** (*boolean*;) – Returns a copy of the dimension dictionary if True (Default value = True)

**Returns** Dictionary of *Dimension* objects.

**Return type** *dict*

**endpoint\_iter** (*\*dim\_strides*, *\*\*kwargs*)

Recursively iterate over the (dimension, stride) tuples specified in *dim\_strides*, returning the start and end indices for each chunk.

For example, the following call effectively produces 2 loops over the ‘ntime’ and ‘nchan’ dimensions in chunks of 10 and 4 respectively.

```
for (ts, te), (cs, ce) in cube.endpoint_iter(('ntime', 10), ('nchan', 4))
    print 'Time range [{ts},{te}] Channel Range [{cs},{ce}].format(
        ts=ts, te=te, cs=cs, ce=ce)
```

**Parameters** **\*dim\_strides** (*list*) – list of (dimension, stride) tuples

**Returns** An iterator producing lists of lower and upper extent tuples [(d0\_low, d0\_high), (d1\_low, d1\_high), ..., (dn\_low, dn\_high)]

**Return type** iterator

**extent\_iter** (*\*dim\_strides*, *\*\*kwargs*)

Recursively iterate over the (dimension, stride) tuples specified in *dim\_strides*, returning the start and end indices for each chunk.

For example, the following call effectively produces 2 loops over the ‘ntime’ and ‘nchan’ dimensions in chunks of 10 and 4 respectively.

```
for (ts, te), (cs, ce) in cube.endpoint_iter(('ntime', 10), ('nchan', 4))
    print 'Time range [{ts},{te}] Channel Range [{cs},{ce}].format(
        ts=ts, te=te, cs=cs, ce=ce)
```

**Parameters** **\*dim\_strides** (*list*) – list of (dimension, stride) tuples

**Returns** An iterator producing lists of lower and upper extent tuples [(d0\_low, d0\_high), (d1\_low, d1\_high), ..., (dn\_low, dn\_high)]

**Return type** iterator

**mem\_required()**

**str** String approximately describing the memory required by arrays registered on the cube, taking their extents into account.

**properties()**

Returns a dictionary of properties

**property** (*name*)

**Parameters** *name* (*str*) – Property to return

**Returns** A property dictionary

**Return type** dict

**register\_array** (*name*, *shape*, *dtype*, *\*\*kwargs*)

Register an array with this cube.

```
cube.register_array("model_vis", ("ntime", "nbl", "nchan", 4), np.complex128)
```

#### Parameters

- **name** (*str*) – Array name
- **shape** (*A tuple containing either Dimension names or ints*) – Array shape schema
- **dtype** – Array data type

**register\_arrays** (*arrays*)

Register arrays using a list of dictionaries defining the arrays.

The list should itself contain dictionaries. i.e.

```
D = [{ 'name': 'uvw', 'shape': (3, 'ntime', 'nbl'), 'dtype': np.float32 },
      { 'name': 'lm', 'shape': (2, 'nsrc'), 'dtype': np.float32 }]
```

**Parameters** *arrays* (*A list or dict.*) – A list or dictionary of dictionaries describing arrays.

**register\_dimension** (*name*, *dim\_data*, *\*\*kwargs*)

Registers a dimension on this cube.

```
cube.register_dimension('ntime', 10000,
                        decription="Number of Timesteps",
                        lower_extent=100, upper_extent=200)
```

#### Parameters

- **dim\_data** (*int or Dimension*) – if an integer, this will be used to define the *global\_size* of the dimension and possibly other attributes if they are not present in *kwargs*. If a *Dimension*, it will be updated with any appropriate keyword arguments
- **description** (*str*) – The description for this dimension. e.g. ‘Number of timesteps’.

- **lower\_extent** (*int*) – The lower extent of this dimension within the global space
- **upper\_extent** (*int*) – The upper extent of this dimension within the global space
- **name** (*Dimension name*) –

**Returns** A hypercube Dimension

**Return type** *Dimension*

**register\_dimensions** (*dims*)

Register multiple dimensions on the cube.

```
cube.register_dimensions([
    {'name': 'ntime', 'global_size': 10,
     'lower_extent': 2, 'upper_extent': 7 },
    {'name': 'na', 'global_size': 3,
     'lower_extent': 2, 'upper_extent': 7 },
])
```

**Parameters** **dims** (*list or dict*) – A list or dictionary of dimensions

**register\_properties** (*properties*)

Register properties using a list defining the properties.

The dictionary should itself contain dictionaries. i.e.

```
D = [
    { 'name': 'ref_wave', 'dtype': np.float32,
      'default': 1.41e6 },
]
```

**Parameters** **properties** (*A dictionary or list*) – A dictionary or list of dictionaries describing properties

**register\_property** (*name, dtype, default, \*\*kwargs*)

Registers a property with this Solver object

```
cube.register_property("reference_frequency", np.float64, 1.4e9)
```

**Parameters**

- **name** (*str*) – The name of this property.
- **dtype** (*Numpy data type*) – Numpy data type
- **default** (*Should be convertible to dtype*) – Default value for this value

**slice\_index** (*\*slice\_dims, \*\*kwargs*)

Returns a tuple of slices, each slice equal to the slice(lower\_extent, upper\_extent, 1) of the dimensions supplied in slice\_dims. If the dimension is integer d, slice(0, d, 1) will be used instead of the lower and upper extents

```
A = np.ones(ntime, na)
idx = cube.slice_index('ntime', 'na', 3)
A[idx].sum()
ntime, na, components = cube.slice_index('ntime', 'na', 3)
A[ntime, na, components].sum()
```

**Parameters** `*slice_dims` (*tuple*) – Tuple of dimensions for which slice objects should be returned.

**Returns** Tuple of `slice(lower, upper, 1)` objects

**Return type** *tuple*

**slice\_iter** (*\*dim\_strides, \*\*kwargs*)

Recursively iterate over the (dimension, stride) tuples specified in `dim_strides`, returning the chunk start offsets for each specified dimensions.

For example, the following call effectively produces 2 loops over the ‘ntime’ and ‘nchan’ dimensions in chunks of 10 and 4 respectively.

```
A = np.ones(size=(100, 4))
for ts, cs in cube.endpoint_iter(('ntime', 10), ('nchan', 4))
    A[ts, cs].sum()

for i in cube.endpoint_iter(('ntime', 10), ('nchan', 4))
    A[i].sum()
```

**Parameters** `*dim_strides` (*list*) – list of (dimension, stride) tuples

**Returns** Iterator producing a tuple of slices for each dimension (`slice(d0_low, d0_high, 1)`, `slice(d1_low, d1_high, 1)`)

**Return type** iterator

**update\_dimension** (*name, \*\*update\_dict*)

Update the dimension size and extents.

**Parameters**

- **\*\*update\_dict** (*: dict: dict*) – A dictionary containing keywords passed through to `update()`
- **name** (*str*) – Name of the dimension to update

**update\_dimensions** (*dims*)

Update multiple dimension on the cube.

```
cube.update_dimensions([
    {'name' : 'ntime', 'global_size' : 10,
     'lower_extent' : 2, 'upper_extent' : 7 },
    {'name' : 'na', 'global_size' : 3,
     'lower_extent' : 2, 'upper_extent' : 7 },
])
```

**Parameters** `dims` (*list or dict:*) – A list or dictionary of dimension updates

## CHAPTER 4

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### Indices and tables

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